

## Roll Number



# INDIAN SCHOOL MUSCAT SECOND PRE-BOARD EXAMINATION MATHEMATICS (041)

CLASS: XII

TERM - II

Time Allotted:2 hours.

02.03.2022

Max. Marks: 40

### **General Instructions:**

- 1. This question paper contains three sections A, B and C. Each part is compulsory.
- 2. Section A has 6 short answer type (SA1) questions of 2 marks each.
- 3. Section B has 4 short answer type (SA2) questions of 3 marks each.
- 4. Section C has 4 long answer type questions (LA) of 4 marks each.
- 5. There is an internal choice in some of the questions.
- 6. Q14 is a case-based problem having 2 sub parts of 2 marks each.

#### **SECTION A**

- 1) Evaluate:  $\int_{-1}^{2} [x] dx$ 
  - 2) Find the general solution of the following differential equations:  $\frac{dy}{dx} = e^{x+y}$

2

2

OR

$$\frac{dy}{dx} + 3y = e^{-3x}$$

3) Find a vector in the direction of vector  $\vec{a} = 3\hat{\imath} + 4\hat{\jmath} - 2\hat{k}$  that has magnitude 13 units.

2

Find the distance of a point (2,5,-3) from the plane  $\vec{r} \cdot (6\hat{i} - 3\hat{j} + 2\hat{k}) = 4$ 

2

5) A fair die is rolled. Consider events  $E=\{1,3,5\}$ ,  $F=\{2,3\}$  and  $G=\{2,3,4,5\}$ , F ind

2

- (i)  $P((E \cup F)/G)$
- (ii)  $P((E \cap F)/G)$
- 6) Two Cards are drawn Simultaneously from a well shuffled deck of cards. Find the probability distribution of the number of successes when getting a spade is considered a success.

2

#### **SECTION B**

7) Evaluate:  $\int \frac{x}{(x-1)(x-2)} dx$ 

3

8) Solve for the particular solution:  $(x^2 - y^2)dx + 2xydy = 0$ ; y(1) = 1

3

9) If  $\vec{a} = \hat{\imath} + 4\hat{\jmath} + 2\hat{k}$ ,  $\vec{b} = 3\hat{\imath} - 2\hat{\jmath} + 7\hat{k}$ ,  $\vec{c} = 2\hat{\imath} - \hat{\jmath} + 4\hat{k}$  then find a vector  $\vec{d}$  which is perpendicular to both  $\vec{a}$  and  $\vec{b}$  &  $\vec{c}$ .  $\vec{d} = 15$ 

OR

If  $\hat{a}$  and  $\hat{b}$  are unit vectors inclined at an angle  $\theta$ , then prove that  $\sin \frac{\theta}{2} = \frac{1}{2} |\hat{a} - \hat{b}|$ 

Find the shortest distance between two lines:  $\vec{r} = \hat{\imath} + 2\hat{\jmath} + 3\hat{k} + \hat{\lambda}(\hat{\imath} - 3\hat{\jmath} + 2\hat{k}) \text{ and } \vec{r} = 4\hat{\imath} + 5\hat{\jmath} + 6\hat{k} + \mu (2\hat{\imath} + 3\hat{\jmath} + \hat{k})$ 

OR

Find x such that the four points A (3,2,1), B (4, x, 5), C (4, 2, -2) and D (6, 5, -1) are coplanar.

**SECTION C** 

11) Evaluate:  $\int_0^{\frac{\pi}{2}} \frac{\sin^2 x}{\sin x + \cos x} dx$ 

4

4

OR

Evaluate:  $\int_{1}^{4} \{|x-1|+|x-2|+|x-3|\} dx$ 

- Find the area of the region enclosed by the parabola  $x^2 = y$ , the line y = x + 2 and the x- axis.
- Find the coordinate of the point P where the line through A(3, -4, -5) and B(2, -3, 1) crosses the plane passing through three points L(2, 2, 1), M(3, 0, 1) and N(4, -1, 0).

CASE-BASED / DATA-BASED

A shopkeeper sells three type of flower seeds: yellow tulips, blue tulips and pink tulips. He sold these seeds as a mixture in the ratio 4: 4: 2, respectively. The germination rates of the three types of seeds are 45%, 60%, and 35% respectively.



- (i) Calculate the probability of a randomly chosen seed to germinate.
- (ii) A seed is selected at random and is found to have germinated, what is the probability that it is a blue tulip seed?

**End of the Question Paper** 

Page 2 of 2



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#### **SECTION A**

2 Evaluate:  $\int_0^1 log\left(\frac{1}{x}-1\right) dx$ 1) 2 2) Find the general solution of the following differential equations:  $\frac{dy}{dx} = e^{x+y}$ **OR**  $\frac{dy}{dx} + 3y = e^{-3x}$ Find a vector in the direction of vector  $\vec{a} = 3\hat{i} + 4\hat{j} - 2\hat{k}$  that has magnitude 13 2 3) units. Find the distance of a point (2,5,-3) from the plane  $\vec{r} \cdot (6\hat{\imath} - 3\hat{\jmath} + 2\hat{k}) = 4$ 2 4) 2 A fair die is rolled. Consider events  $E=\{1,3,5\}$ ,  $F=\{2,3\}$  and  $G=\{2,3,4,5\}$ , Find 5)  $P((E \cup F)/G)$ (i)  $P((E \cap F)/G)$ (ii) Two Cards are drawn Simultaneously from a well shuffled deck of cards. Find the 6) probability distribution of the number of successes when getting a spade is considered a success. **SECTION B** 

7) Evaluate: 
$$\int \frac{x}{(x+1)(x+2)} dx$$

Solve for the particular solution : 
$$(x^2 - y^2)dx + 2xydy = 0$$
;  $y(1) = 1$ 

9) If 
$$\vec{a} = \hat{\imath} + 4\hat{\jmath} + 2\hat{k}$$
,  $\vec{b} = 3\hat{\imath} - 2\hat{\jmath} + 7\hat{k}$ ,  $\vec{c} = 2\hat{\imath} - \hat{\jmath} + 4\hat{k}$ , then find a vector  $\vec{d}$  which is perpendicular to both  $\vec{a}$  and  $\vec{b}$  &  $\vec{c} \cdot \vec{d} = 15$ 

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If  $\hat{a}$  and  $\hat{b}$  are unit vectors inclined at an angle  $\theta$ , then prove that  $\sin \frac{\theta}{2} = \frac{1}{2} |\hat{a} - \hat{b}|$ 

Find the shortest distance between two lines:  $\vec{r} = \hat{\imath} + 2\hat{\jmath} + 3\hat{k} + \hat{\lambda}(\hat{\imath} - 3\hat{\jmath} + 2\hat{k}) \text{ and } \vec{r} = 4\hat{\imath} + 5\hat{\jmath} + 6\hat{k} + \mu (2\hat{\imath} + 3\hat{\jmath} + \hat{k})$ 

#### OR

Find x such that the four points A (3, 2, 1), B(4, x, 5). C (4, 2, -2) and D (6, 5, -1) are coplanar.

# **SECTION C**

11) Evaluate:  $\int_0^{\frac{\pi}{2}} \frac{\cos^2 x}{\sin x + \cos x} \ dx$ 

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4

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3

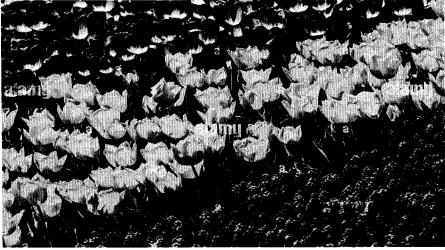
OR

Evaluate:  $\int_{1}^{4} \{|x-1| + |x-2| + |x-3|\} dx$ 

- Find the area of the region enclosed by the parabola  $x^2 = y$ , the line y = x + 2 and the x- axis.
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- (i) Calculate the probability of a randomly chosen seed to germinate.
- (ii) A seed is selected at random and is found to have germinated, what is the probability that it is a blue tulip seed?

**End of the Question Paper** 



SET C



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### SECTION A

2 Evaluate:  $\int_{-1}^{1} e^{|x|} dx$ 1) 2 Find the general solution of the following differential equations: 2)  $\frac{dy}{dx} = e^{x-y}$ OR  $\frac{dy}{dx} + 3y = e^{3x}$ Find a vector in the direction of vector  $\vec{a} = 3\hat{\imath} + 4\hat{\jmath} - 2\hat{k}$  that has magnitude 13 units. 2 3) Find the distance of a point (2,53) from the plane  $\vec{r} \cdot (6\hat{\imath} - 3\hat{\jmath} + 2\hat{k}) = 4$ 2 4) 2 Given that events A and B are such that P(A)=1/2, P(B)=p, 5)  $P(A \cup B) = 3/5$ . Find p if they are (i) Mutually exclusive (ii) independent. Two Cards are drawn Simultaneously from a well shuffled deck of cards. Find the 2 6) probability distribution of the number of successes when getting a spade is considered a success.

#### **SECTION B**

7) Evaluate: 
$$\int \frac{x}{(x+1)(x+2)} dx$$

8) Solve for the particular solution : 
$$(x^2 - y^2)dx + 2xydy = 0$$
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9) 
$$\vec{a} = \hat{\imath} + 4\hat{\jmath} + 2\hat{k}$$
,  $\vec{b} = 3\hat{\imath} - 2\hat{\jmath} + 7\hat{k}$ ,  $\vec{c} = 2\hat{\imath} - \hat{\jmath} + 4\hat{k}$ , Find a vector  $\vec{d}$  which is perpendicular to both  $\vec{a}$  and  $\vec{b}$  &  $\vec{c}$ .  $\vec{d} = 15$ 

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10) Find the shortest distance between two lines:

 $\vec{r} = \hat{\imath} - 2\hat{\jmath} + 3\hat{k} + \hat{\lambda}(-\hat{\imath} + \hat{\jmath} - 2\hat{k})$  and  $\vec{r} = \hat{\imath} - \hat{\jmath} - \hat{k} + \mu (\hat{\imath} + 2\hat{\jmath} - 2\hat{k})$ 

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11) Evaluate:  $\int_0^{\frac{\pi}{2}} \frac{\sin^2 x}{\sin x + \cos x} \ dx$ 

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OR

Evaluate:  $\int_{1}^{4} \{|x-1| + |x-2| + |x-3|\} dx$ 

- 12) Find the area bounded by the curve  $x^2 = 4y$  and the line x = 4y 2
- Find the coordinate of the point P where the line through A(3, -4, -5) and B(2, -3, 1) crosses the plane passing through three points L(2, 2, 1), M(3, 0, 1) and N(4, -1, 0).

CASE-BASED/DATA-BASED

In answering a question on a multiple-choice test for class XII, a student either knows the answer or guesses. If 3/5 is the probability that he knows the answer and 2/5 be the probability that he guesses. Assume that a student who guesses at the answer will be correct with probability 1/3.



Based on the given information, answer the following questions.

A randomly selected question is attempted by the student

- (i) What is the probability that the student answered it correctly?
- (ii) What is the probability that the student knows the answer given that he answered it correctly?

**End of the Question Paper**